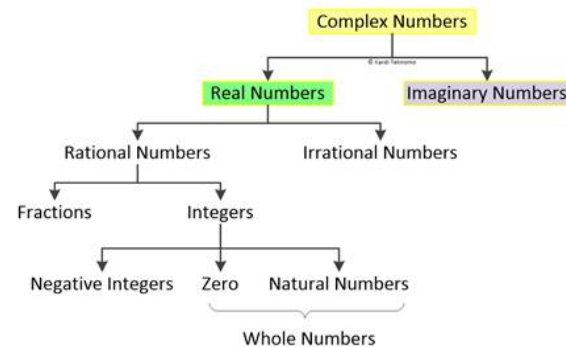


Math 2

Imaginary Numbers

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## I. The Complex Number Tree



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## II. Rational vs. Irrational

Rational Numbers:

These are numbers such as  $\frac{2}{7}$ ,  $\frac{3}{4}$ , and  $-9$  that can be written as the ratio of two integers. When written as decimals, rational numbers terminate or repeat.

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Irrational Numbers:

Real numbers that are not rational, such as  $\sqrt{2}$  and  $\pi$ . When written as decimals, irrational numbers do not terminate and do not repeat.

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Identify each question as Rational or Irrational.

1.  $\sqrt{11}$

2.  $\sqrt{25}$

3.  $0.\overline{66}$

4.  $\sqrt{5}$

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### III. Complex Numbers

All numbers are complex.

There is a special subset of them that we call imaginary.

Imaginary numbers solve the issue of negative numbers under a square root.

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### Imaginary Numbers

$$\sqrt{-36}$$

$$\sqrt{-1} = i$$

$$i =$$

$$i^2 =$$

$$i^3 =$$

$$i^4 =$$

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$$\sqrt{-25}$$

$$\sqrt{-45}$$

$$\sqrt{-8}$$

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"Pop out the *i*'s before you multiply or simplify."

$$\sqrt{-2} \cdot \sqrt{-8} \qquad \sqrt{-5} \cdot \sqrt{-15}$$

$$\sqrt{-6} \cdot \sqrt{3} \qquad (-2\sqrt{-8})(3\sqrt{-2})$$

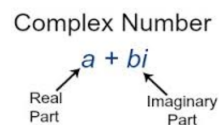
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$$(6\sqrt{-24})(-3\sqrt{6}) \qquad \frac{36i}{4i}$$

$$(-5i)^2$$

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#### IV. Operations with Complex Numbers



Write each number in complex number form.

1.  $2 + \sqrt{-3}$

2.  $6 - \sqrt{-28}$

3.  $-\sqrt{-50} - 2$

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Adding and Subtracting, we can only add the parts that are alike:

Examples:

1.  $(11+5i)+(3+2i)$

2.  $(18-3i)-(12-i)$

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Multiplying, we treat them just like a polynomial! Be sure to clean up any imaginary numbers raised to a power.

1.  $(10 + 7i)(2 + 3i)$

2.  $(5 - 6i)(9 + 3i)$

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### You Try!

1)  $(4 + 3i) + (-6 - 2i)$

2)  $(-4 - 2i) - (-6 + 8i)$

3)  $(7 - 7i) - (1 - 7i)$

4)  $(-7i)(5i)(5 + 3i)$

5)  $(-8 - 4i)(6 + 5i)$

6)  $(1 - 3i)^2$

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### Using Imaginary #'s to Solve!

1.  $x^2 + 36 = 0$

2.  $4x^2 + 9 = 0$

3.  $3x^2 + 10 = -6x^2 + 9$

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